

Duration: 3hrs

- N.B.: (1) Question No 1 is Compulsory.
(2) Attempt any three questions out of the remaining five.
(3) All questions carry equal marks.
(4) Assume suitable data, if required and state it clearly.

Attempt any FOUR

[20]

- a Sketch its even and odd parts of:

$$x(t) = \frac{2}{5}t u(t) \dots \dots 0 \leq t \leq 5$$

- b Consider a discrete time system shown in Fig. 1

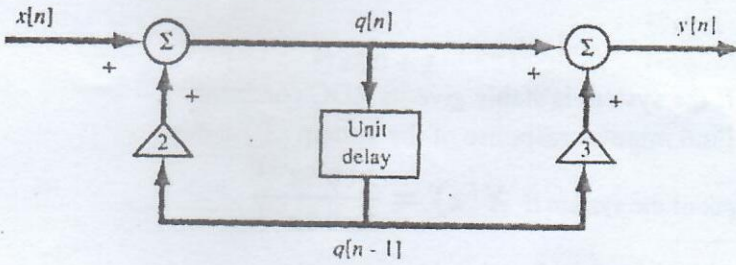


Fig 1

Write the difference equation for this system which relates the output $y(n)$ with input $x(n)$. Also state whether the system is FIR or IIR.

- c Obtain the Laplace transform of the given Square wave (Fig 2)

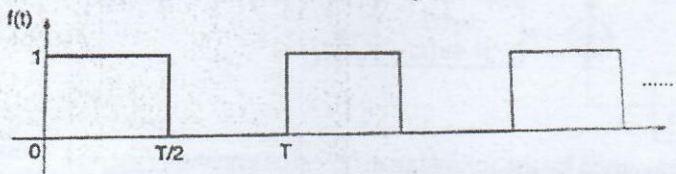


Fig. 2.

- d Explain the Gibb's phenomenon and the conditions necessary for the convergence of the Fourier Series
e Discuss the limitations of Fourier Transform.

- 2 a A certain system has the impulse response $h(t)$ and input $x(t)$ as shown in Fig 3.

[10]

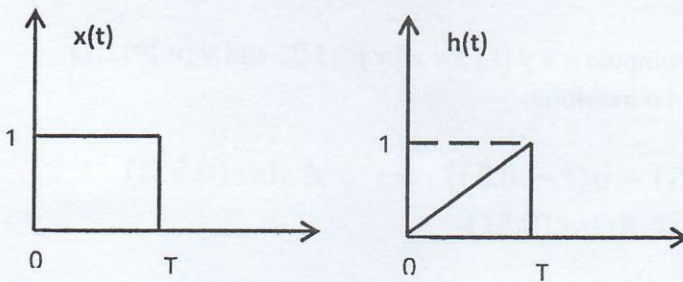


Fig. 3

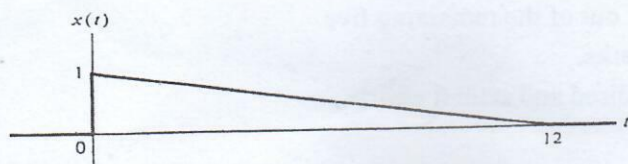
Obtain the output for the given system without using any transform.

- b Classify the following systems as Linear/nonlinear, time variant / invariant Causal/Noncausal and static/dynamic.

[10]

- $y[n] = x[n^2]$
- $y(t) = x(t) + x(t+2)$

- 3 a For the given signal $x(t)$ [10]



Sketch

1. $x(1-t)[u(t+1) - u(t-2)]$
2. $x(t)[\delta(t - \frac{3}{2})]$

- b A causal LTI system has a transfer function $H(z) = H_1(z) \cdot H_2(z)$ where [10]

$$H_1(z) = \frac{1 - 0.2z^{-1}}{1 + 0.5z^{-1}} \quad \text{and} \quad H_2(z) = \frac{1}{1 + 0.3z^{-1}}$$

- i. If the system is stable give its ROC condition.
- ii. Find impulse response of the system

Find the output of the system if $X(z) = \frac{1 + 0.3z^{-1}}{1 - 0.2z^{-1}}$

- 4 a An audio tone $x(t)$ is passed through a two band audio equalizer followed by amplifier as shown in Fig.4. Obtain the Overall Transfer function of this system using Laplace transform. [10]

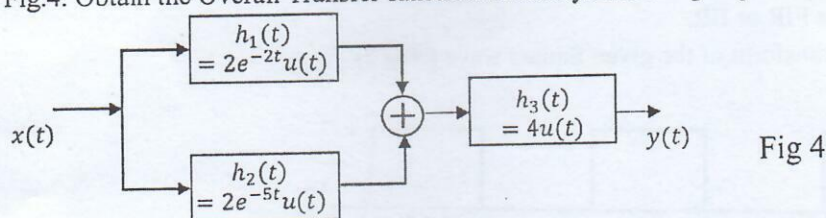


Fig 4

- b A second order RC filter is governed by the following differential equation [10]

$$\frac{d^2y(t)}{dt^2} + 5\frac{dy}{dt} + 4y(t) = \frac{dx(t)}{dt}$$

Obtain the filtered output if the input signal is $x(t) = e^{-2t}u(t)$,

Assume initial conditions $y(0) = 1; \frac{dy}{dt}\bigg|_{t=0} = 1$

- 5 a Define cross-correlation and compute $r_{xy}[l]$ for $x[n] = \{1, 2\}$ and $y[n] = \{2, 1\}$ [10]
 b State the duality theorem of Fourier transform. [10]

If the Fourier transform of

$$A[u(t + 0.5) - u(t - 0.5)] \leftrightarrow A \operatorname{sinc}(0.5 \Omega)$$

Then find the Fourier transform of $A \operatorname{sinc}(0.5t)$

- 6 Write short notes on [20]

- a ROC of Z transform
- b Properties of Autocorrelation
- c Difference between FIR and IIR filters
- d Properties of Laplace transform
