

Time:

Marks: 80

N.B. : (1) Question Number 1 is compulsory (2) Solve any three questions from the remaining questions

3) Make suitable assumptions if needed

4) Assume appropriate data whenever required. State all assumptions clearly.

1. a. Explain the following terms partition set with suitable example. 5
 1. Partition set
 2. Disjoint sets
- b. Construct the Truth Table and check if the following statement is tautology. 5
 $(P \rightarrow Q) \leftrightarrow (\neg Q \rightarrow \neg P)$
- c. Let $f: A \rightarrow B$ be a Function from A to B. Prove that f^{-1} exists if and only if f is a Bijective Function. 5
- d. Prove by mathematical induction that $x^n - y^n$ is divisible by $x - y$ 5
- 2 a. Define Equivalence Relation. A relation R is called circular if aRb and bRc imply cRa . Show that R is circular if and only if it is an Equivalence Relation 8
- b. Let $A = \{1, 2, 3, 4\}$ and $R = \{(1, 1), (1, 2), (1, 4), (2, 4), (3, 1), (3, 2), (4, 2), (4, 3), (4, 4)\}$. Find Transitive Closure of R using Warshall's algorithm. 8
- c. Let $f: \mathbb{R} \rightarrow \mathbb{R}$ be a function defined by $f(x) = 2x - 3$. Prove that it is Bijective & find inverse. 4
- 3 a. Let f, g, h be functions on real numbers \mathbb{R} defined as follows: $f(x) = 2x + 5$, $g(x) = 5x + 3$, $h(x) = 3x$
 Find: 1) $f \circ g$ 2) $g \circ f$ 3) $g \circ h$ 4) $f \circ g \circ h$ 5) $g \circ f \circ h$ 8
- b. Give the generating function for the following sequences 8
 1) $\{0, 1, 2, 3, 4, \dots\}$
 2) $\{1, 2, 3, 4, 5, \dots\}$
 3) $\{2, 2, 2, 2, 2, \dots\}$
 4) $\{0, 0, 0, 1, 1, 1, \dots\}$